Colombian Women's Life Patterns: A Multivariate Density Regression Approach

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Introduction

- Goal is to make predictions for multivariate system in a Bayesian framework
- Framework is complicated as it has to reliably take multivariate input
- The case study used in the article as an example is survey data of Columbian women

The Data

Variety of discrete, categorical or binary data types

Predictors:

- x1 Age at interview
- x2 Area (urban/rural)
- x3 Region (in Columbia)
- x4 Family Violence

Responses:

- z1 Age at Sexual Debut
- z2 Age at Union
- z3 Age at First Child
- z4 Work Status

The Method

- Goal of the method is ambitious;
 - Be able to give correlated, multivariate input
 - Be adaptable to different data sizes and types

The Method

Combination of different methods:

- Adaptive Markov Chain Monte Carlo (aMCMC)
 - Gibbs Sampling
 - Metropolis Hastings
 - Fixed Truncation
- Sequential Monte Carlo (SMC)
 - Adaptive truncation

Transformation of Data to Suit the Method

Link functions

$$z_{\ell} = h_{\ell}(\mathbf{y}, \mathbf{x}) = c_{\ell}(\mathbf{y}, \mathbf{x}) \lfloor \exp(y_{\ell}) \rfloor, \quad \text{for } \ell = 1, 2,$$

$$z_{3} = h_{3}(\mathbf{y}, \mathbf{x}) = \mathbb{1}_{[0,\infty)}(y_{3}),$$

Inverse Link functions

$$(l_{\ell}, u_{\ell}) = \begin{cases} (\log(x_1 + 1), \infty) & \text{for censored } z_{\ell} = 0\\ (\log(z_{\ell}), \log(z_{\ell} + 1)) & \text{for uncensored } z_{\ell} \neq 0 \end{cases}, \text{ when } \ell = 1, 2,$$
$$(l_3, u_3) = \begin{cases} (-\infty, 0) & \text{for } z_3 = 0\\ (0, \infty) & \text{for } z_3 = 1 \end{cases}.$$

Gibbs Sampling

- Useful for multivariate distributions
- The joint: P(x,y) is difficult to sample
- The conditionals: P(x|y) and P(y|x) are easier to sample. One variable is updated at a time, the other is fixed.
- When conditionals are unknown we add a Metropolis-Hastings step.



Truncation Level and SMC

• The truncation level is fixed for the aMCMC:

the predictive model is a mixture of a fixed number of component models

• The truncation level is adaptive SMC:

SMC samples component models from aMCMC output

the number of components is chosen by balancing computational burden and quality of approximation to an infinite-dimensional model

Results

An example of the type of results as given by the model



Figure 6: Predictive densities of the ages at union and first child as functions of Age for women who grew up in violent (\mathbf{P}, \mathbf{B}) and non-violent ($\mathbf{\bar{P}}, \mathbf{\bar{B}}$) families. Results are reported for urban and rural areas of the least developed region (Territorios nacionales) and for the capital (Bogota). The region above the dashed line indicates when age at event exceeds Age. The black line is the posterior median function.

Results

An example of the type of results as given by the model

