What is shape?

Characterizing particle morphology using genetic algorithms and deep generative models

A review by Simon Guldager Andersen

UNIVERSITY OF COPENHAGEN



ORIGINAL PAPER



What is shape? Characterizing particle morphology with genetic algorithms and deep generative models

R. Buarque de Macedo¹ · S. Monfared¹ · K. Karapiperis² · J. E. Andrade¹

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Abstract

Engineered granular materials have gained considerable interest in recent years. For this substance, the primary design variable is grain shape. Optimizing grain form to achieve a macroscopic property is difficult due to the infinite-dimensional function space particle shape inhabits. Nonetheless, by parameterizing morphology the dimension of the problem can be reduced. In this work, we study the effects of both intuitive and machine-picked shape descriptors on granular material properties. First, we investigate the effect of classical shape descriptors (roundness, convexity, and aspect ratio) on packing fraction ϕ and coordination number Z. We use a genetic algorithm to generate a uniform sampling of shapes across these three shape parameters. The shapes are then simulated in the level set discrete element method. We discover that both ϕ and Z decrease with decreasing convexity, and Z increases with decreasing aspect ratio across the large sampling of morphologies—including among highly non-convex grains not commonly found in nature. Further, we find that subtle changes in mesoscopic properties can be attributed to a continuum of geometric phenomena, including tessellation, hexagonal packing, nematic order and arching. Nonetheless, such descriptors alone can not entirely describe a shape. Thus, we find a set of 20 descriptors which uniquely define a morphology via deep generative models. We show how two of these machine-derived parameters affect ϕ and Z. This methodology can be leveraged for topology optimization of granular materials, with applications ranging from robotic grippers to materials with tunable mechanical properties.

Keywords Granular materials \cdot Non-convex \cdot Topology optimization \cdot Deep generative models \cdot Discrete element method \cdot LS-DEM

Structure of the presentation

- I. Setting the stage
- II. Genetic algorithms generally and specifically
- III. Variational autoencoders a very brief introduction
- IV. Results and discussion
- V. Questions?

Genetic algorithms are the main focus of this presentation

I. ~ Setting the stage

What we want: Predict the grain shape needed to give a granular material certain physical properties specified by us

How we'll do it:

- \rightarrow Create many particle shapes with a genetic algorithm
- \rightarrow Use these to train a VAE to construct a basis for grain shape
- \rightarrow For each grain shape of interest, simulate the interaction of many identical grains to extract bulk properties
- \rightarrow Understand the mapping between the basis and bulk material properties

II. ~ Genetic algorithms - Overview

- Stochastic global optimization scheme
- Biased towards better solutions, but allows for worse to avoid getting stuck in local minima
- Many hyperparameters careful and patient tuning necessary

II. ~ Genetic algorithms - Stages

Initialize a population of N solutions (randomly or using prior knowledge)

At each iteration (not necessarily in this order):

- **1) Fitness evaluation & Selection:** Evaluate the quality of each solution and select k solutions through a selection scheme. Discard the rest
- **2) Crossover:** Produce N-k new solutions by combining the current k solutions through a crossover scheme
- **3) Mutation:** Mutate each solution with probability p through a mutation scheme

Terminate when convergence criterion or max iterations are met

II. ~ Genetic algorithms – Selection stage

Fitness evaluation – *evaluate the quality of all solutions:*

- $\circ~$ 'Quality' is quantified by the cost function
- Incorporate prior knowledge into the cost function, e.g. by adding penalty terms for non-physical solutions

Selection – *select k individuals through a selection scheme like e.g.:*

- \circ Roulette wheel selection
- Tournament selection

II. ~ Genetic algorithms – Crossover stage

Crossover stage – *Produce N-k new solutions by combining the current k solutions through a crossover scheme:*

 \circ Pick two solutions at random and crossover with probability p_c

Crossover scheme examples:

- Linear combinations of two or more solutions
- Swapping one or more components of two solutions

Swapping Example; crossover at the second index:

Parent 1 = $(x_1, x_2, x_3, x_4, x_5)$, Parent 2 = $(y_1, y_2, y_3, y_4, y_5)$ yielding

Child $1 = (y_1, y_2, x_3, x_4, x_5)$, Child $2 = (x_1, x_2, y_3, y_4, y_5)$

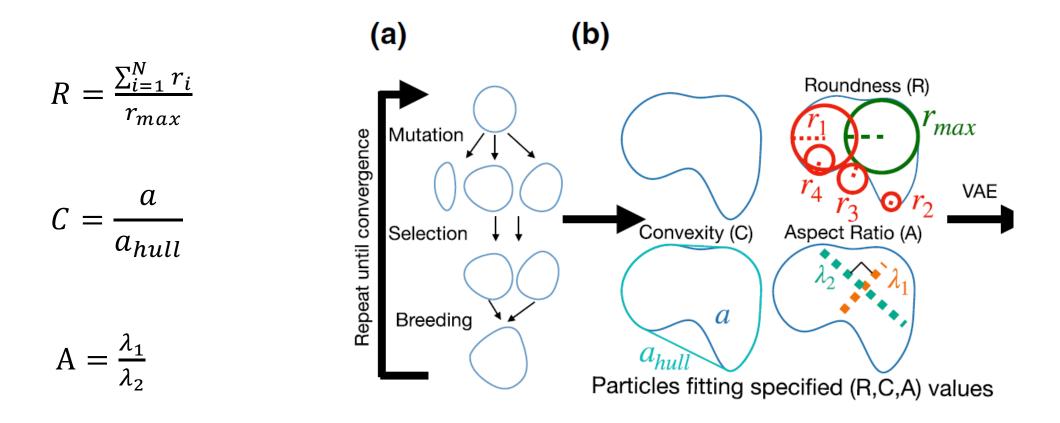
II. ~ Genetic algorithms – Mutation stage

Mutation stage – Mutate each solution with probability p_m through a mutation scheme:

- Perturb one or more components by a random value(s) drawn by some distribution
 - \rightarrow Gaussian results in mostly small steps
 - \rightarrow Lévy results in small steps combined with occasional big jumps

II. ~ Using GAs for particle generation

Which parameters are relevant to the shape of a 2D object?



II. ~ What does the cost function look like?

$$cost = (C - C_{target})^{2} + (R - R_{target})^{2} + (A - A_{target})^{2} + 100 \cdot SC + 100 \, SI + 100 \, BN$$

$$SC = \begin{cases} 1, & \text{if any corner is too sharp} \\ 0, & \text{otherwise} \end{cases}$$

$$SI = \begin{cases} 1, & \text{if particle self - intersects} \\ 0, & \text{otherwise} \end{cases}$$

$$BN = \begin{cases} 1, & \text{if points of opposite side are too close} \\ 0, & \text{otherwise} \end{cases}$$

II. ~ Generate particle with a given (R, C, A)

Initialize N = 50 particles, each one as 8 points uniformly distributed on an ellipse with aspect ratio A

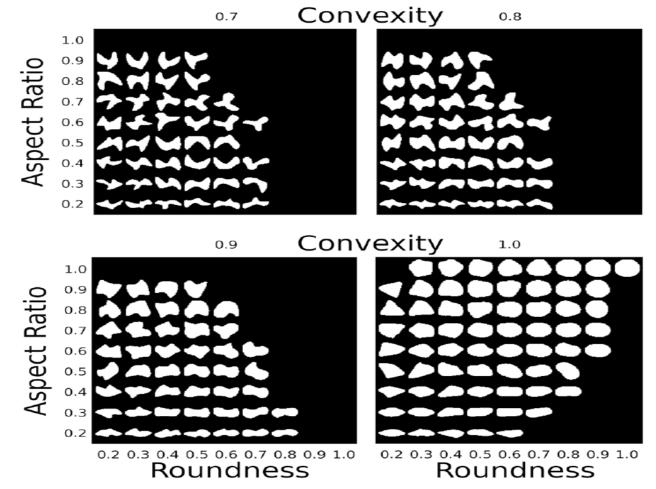
At each iteration:

- **Breed** k new solutions by choosing solution pairs at random with $p_c = 0.2$ and randomly swapping points.
- **Mutate** each particle point (r, θ) with $p_m = 0.5$ by drawing values from Gaussians specified by $(\mu_r = 0, \sigma_r = 1)$ and $(\mu_\theta = 0, \sigma_{theta} = 0.05)$
- Select the best ~ $\frac{N+k}{2}$ solutions by tournament selection. Duplicate the winners until the population size is 50

Terminate when the minimum cost of a solution is less than 0.0005

II. ~ Examples of generated particles

The point of everything so far has been to create 10,000 unique images as training data for the VAE



III. ~ Variational autoencoders – *very* briefly

- Deep generative model
- Dimensionality reduction
- Latent space distribution

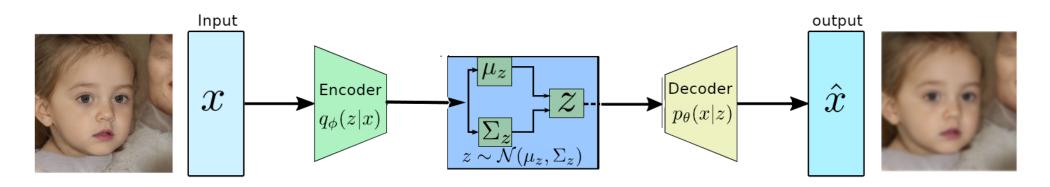
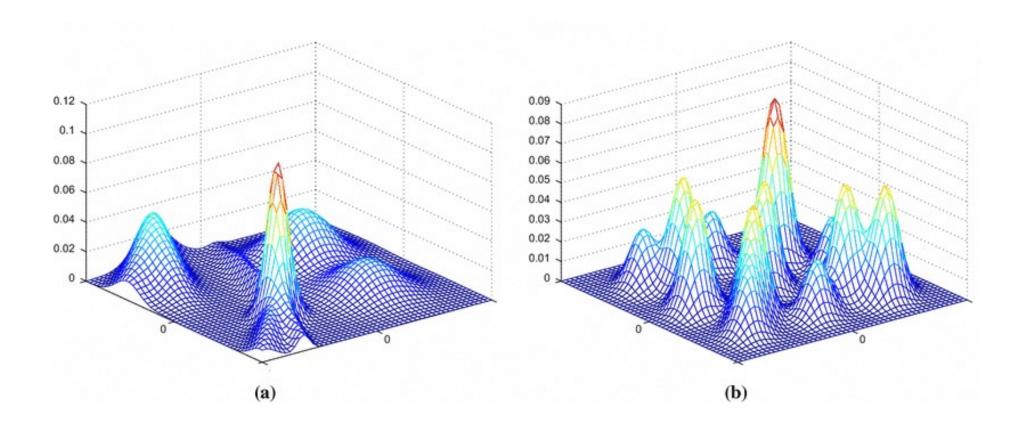


Image by Sunil Yadav

III. ~ Variational autoencoders – very briefly

Possible latent distributions of a 2 dimensional latent space



III. ~ Constructing a space of possible shapes

- o Generate 10,000 unique images of particle shape as training data
- Assume that training data roughly 'maps out' true shape space \rightarrow i.e. no important regions of shape space without images
- During traning, the VAE learns to interpolate between shapes
- After training, the VAE maps any latent vector to a unique shape
 - ightarrow In this sense, we have built a space of possible grain shapes

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III. ~ Training a VAE with the GA-shapes

- Trained on the 10,000 images of particle shapes
- A 20-dimensional latent space enough for accurate reconstruction
- Unphysical shapes when $z_i \notin [-4,4]$, i = 1, ..., 20
- Using just 10 subdivisions per dimension $\rightarrow 10^{20}$ unique shapes

IV. ~ Results and discussion

- Having constructed space for possible grain shapes, mapping to bulk properties can in principle be obtained
 - \rightarrow Many simulations needed to establish relationships
 - \rightarrow Not given that each dimension has a simple physical interpretation

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