Applied ML Clustering Algorithms





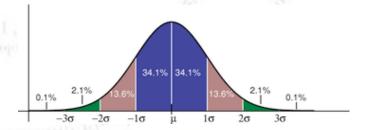


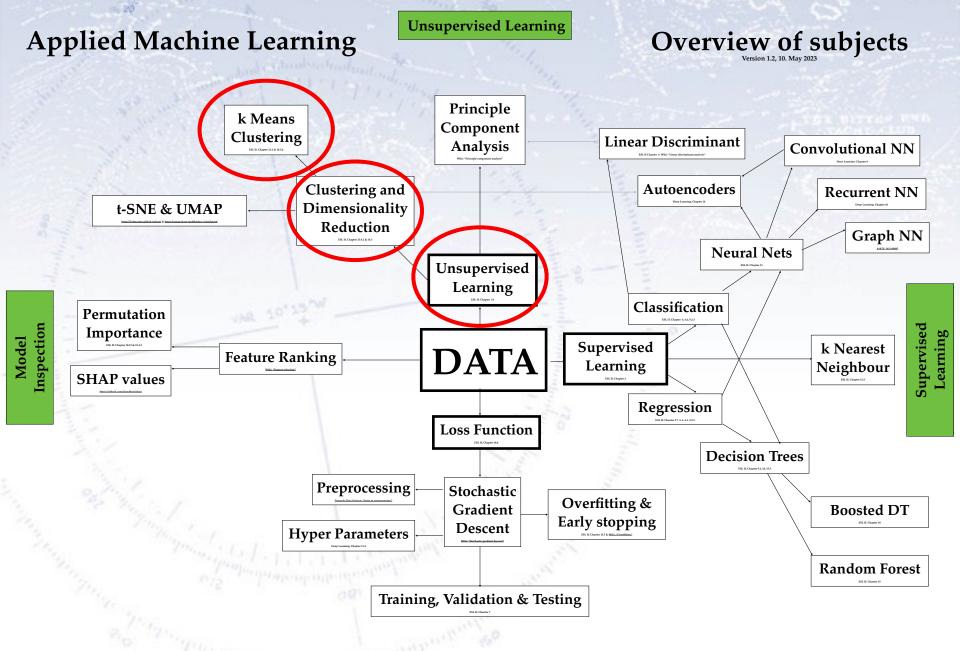






Troels C. Petersen (NBI)



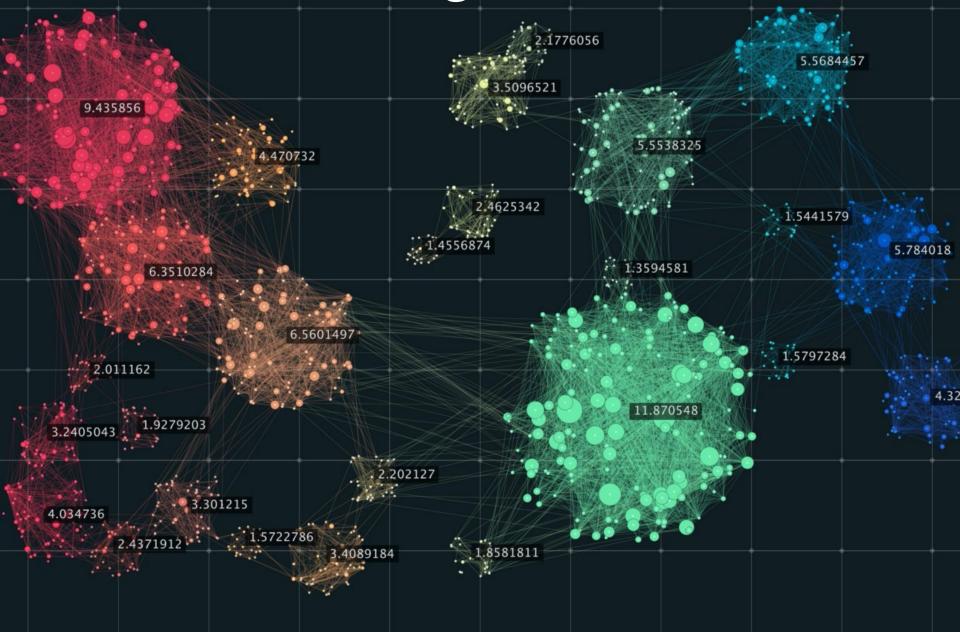


References:

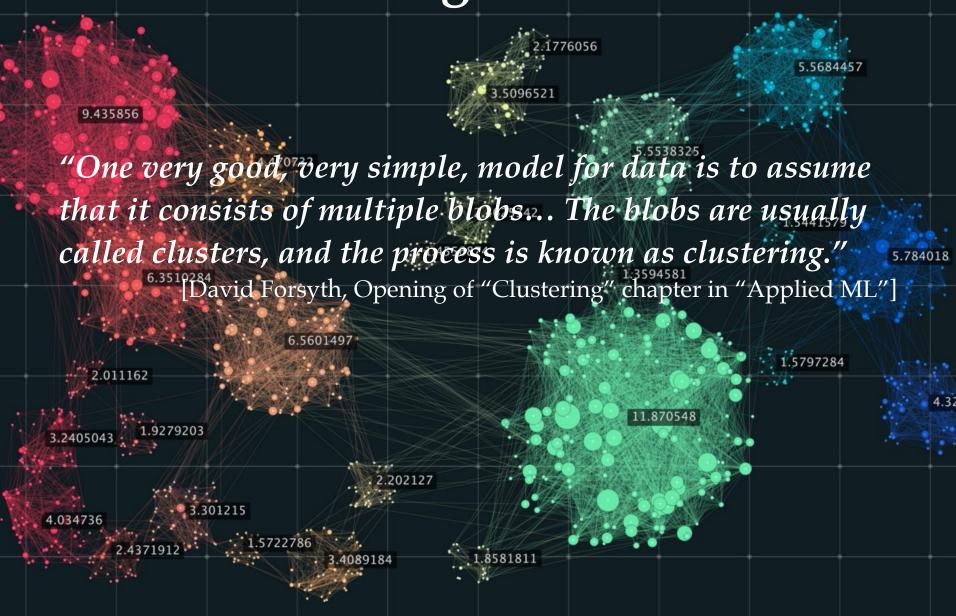
Trevor Hastie et al.: "Elements of Statistics Learning II" (ELS II) Ian Goodfellow et al.: "Deep Learning"

Wiki: Good reference for most subjects (only specified when essential) Various blogs/githubs/papers for specific subjects.

Clustering... is an art!



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The concept of clustering

Clustering is one of the two main "unsupervised" ML methods (the other being dimensionality reduction). It is to some extend related to classification much like dimensionality reduction is related to regression.

"Clusters presumably reflect some mechanism at work in the domain from which instances are drawn, a mechanism that causes some instances to bear a stronger resemblance to each other than they do to the remaining instances."

[Pages 141-142, Data Mining: Practical Machine Learning Tools and Techniques, 2016.]

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Important: It is mandatory to first transform the input variables, so that mean and variances are of order zero and unity.

Evaluating clustering

Evaluation of identified clusters is subjective and may require a domain expert, although many clustering-specific quantitative measures do exist.

Typically, clustering algorithms are compared on synthetic datasets with predefined clusters, which an algorithm is expected to discover.

"Clustering is an unsupervised learning technique, so it is hard to evaluate the quality of the output of any given method."

[Page 534, Machine Learning: A Probabilistic Perspective, 2012.]

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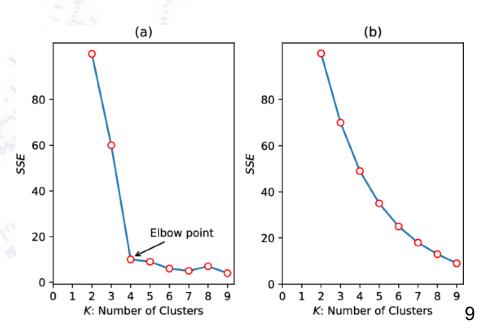
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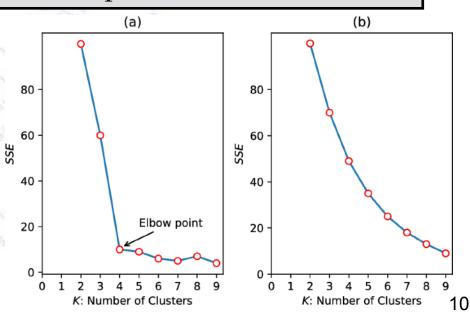
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One way of visually evaluating a clustering algorithm is to combine it with a dimensionality reduction, though one then observes the combined performance of the two.

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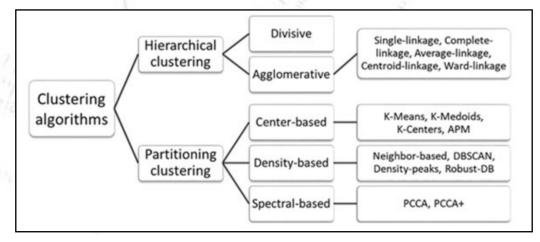
Clustering algorithms

Clustering is an "old field" and many philosophies (and algorithms) have been developed. They can roughly be reduced to two approaches:

- **Hierarchical clustering** algorithms are based on recursively either merging smaller clusters in to larger ones or dividing larger clusters to smaller ones.
- **Partitioning clustering** algorithms generate various partitions and then iteratively place each instance best in one of k mutually exclusive clusters.

Hierarchical clustering does not require any input parameters, while partitioning clustering algorithms require the number of clusters to start running. Hierarchical clustering returns a much more meaningful and subjective division of clusters but partitioning clustering results in exactly k

clusters.

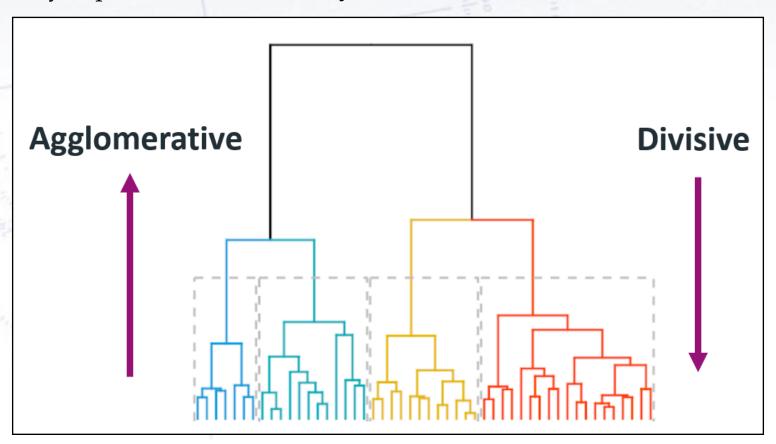


Hierarchical clustering algorithms

Hierarchical clustering algorithms can be further divided:

- **Agglomerative**: Merge smaller clusters into larger ones
- **Divisive**: Divide larger clusters into smaller ones.

The only requirement is a **similarity measure** to decide distance between cases.



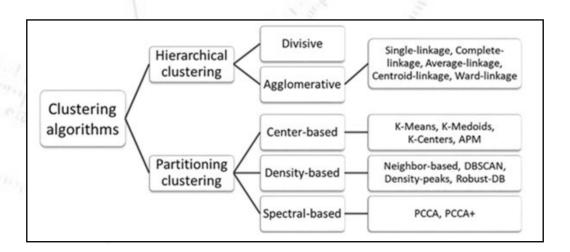
Partitioning clustering algorithms

Partitioning clustering algorithms can (also) be further divided:

- Center-based: Build clusters around (random?) centers (k-Means).
- **Density-based**: Build clusters around (high) densities (**DBSCAN**).
- **Spectral-based**: Uses eigenvalues of the similarity matrix to perform dimensionality reduction before clustering (**PCCA+**).

"k-Means clustering is the "go-to" clustering algorithm. You should see it as a basic recipe from which many algorithms can be concocted."

[David Forsyth, "Applied ML" chapter 8.2.6]

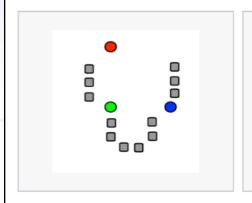


k-Means clustering

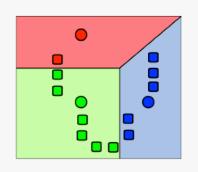
The recipe is to iterate the below points, until movements are "small":

- Allocate each data point to the closest cluster center
- Re-estimate cluster centers from their data points.

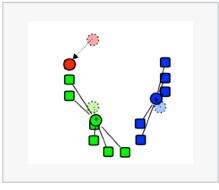
Demonstration of the standard algorithm



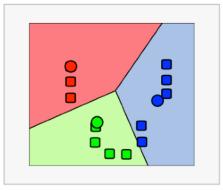
1. *k* initial "means" (in this case *k*=3) are randomly generated within the data domain (shown in color).



 k clusters are created by associating every observation with the nearest mean. The partitions here represent the Voronoi diagram generated by the means.



The centroid of each of the k clusters becomes the new mean.



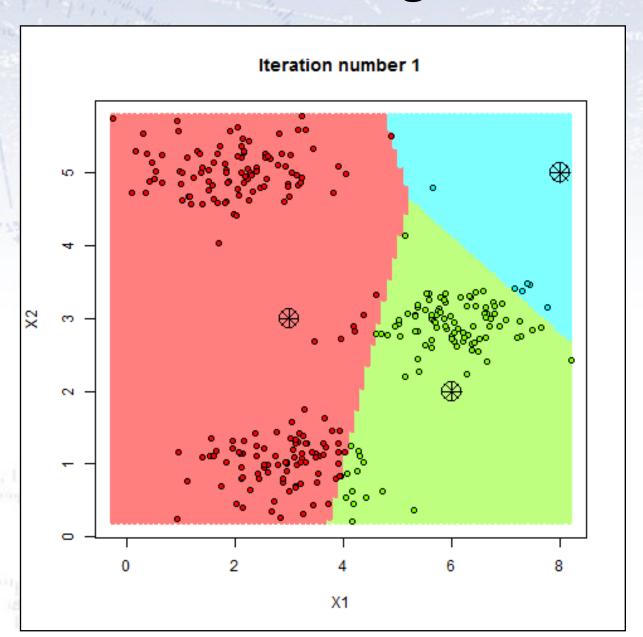
 Steps 2 and 3 are repeated until convergence has been reached.

There are many variations, improvements, etc. that refines this algorithm. Most notably are the k-means++ (better initial points) and k-mediods methods.

k-Means clustering

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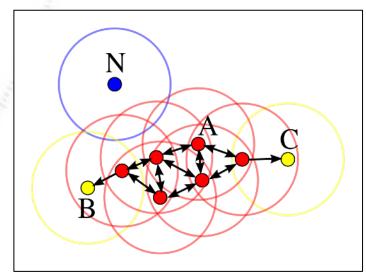
DBSCAN algorithm

DBSCAN classifies points as core points, reachable points and outliers:

- A point p is a **core point** if at least minPts points are within distance ε of it.
- A point q is **directly reachable** from p if point q is within distance ε from core point p. Points are only said to be directly reachable from core points.
- A point q is **reachable** from p if there is a path p_1 , ..., p_n with $p_1 = p$ and $p_n = q$, where each p_{i+1} is directly reachable from p_i . Note that this implies that the initial point and all points on the path must be core points, with the possible exception of q.
- All points not reachable from any other point are outliers or noise points.

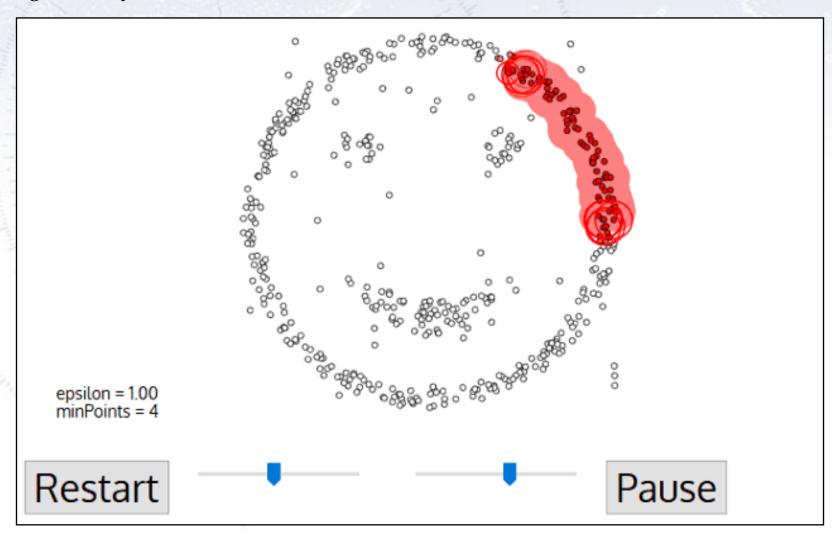
DBSCAN has two parameters: minPts and ε .

If p is a core point, then it forms a cluster together with all points (core or non-core) that are reachable from it. Each cluster contains at least one core point; non-core points can be part of a cluster, but they form its "edge", since they cannot be used to reach more points.



DBSCAN algorithm

As can be seen, DBSCAN is a rather generic algorithm, capable of handling a large variety of data.



Expectation-Maximisation algorithm

The Expectation–Maximisation (EM) algorithm is an iterative method to find maximum likelihood estimates of parameters, where the model depends on unobserved latent variables.

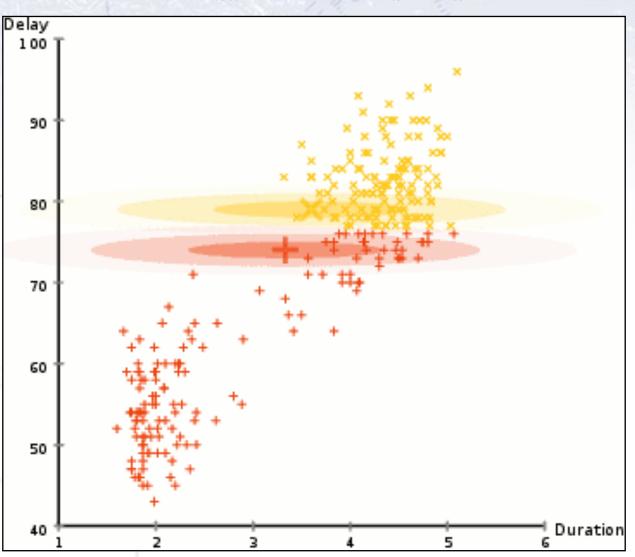
Based on the notion that data falls in "blobs", the model used in clustering is typically a Gaussian Mixture Model.

The EM algorithm alternates between performing an expectation (E) step, calculating the expected likelihood given current parameters, and a maximisation (M) step, computing new parameters maximising the expected likelihood found on the E step:

- 1. First, initialise the parameters θ to some random values.
- 2. Compute the probability of each possible likelihood value, given θ .
- 3. Use the just-computed likelihood values to compute a better estimate for the parameters θ . Iterate steps 2 and 3 until convergence.

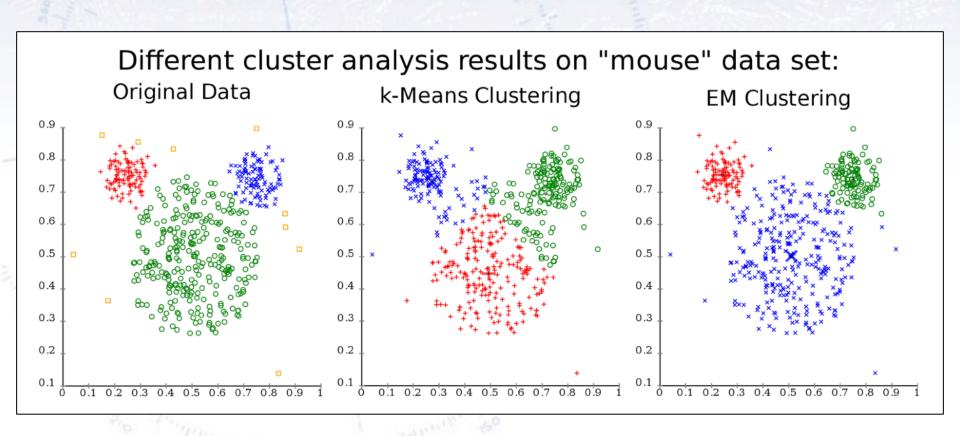
Expectation Maximisation algorithm

An example is shown below, applied to the eruption pattern of "Old Faithful".



The "Mickey Mouse" test

The recipe is: iterate: allocate each data point to the closest cluster center; reestimate cluster centers from their data points.



Distance Metric & Silhouette score

A typical clustering metric is the average distance to **the center of the cluster that a point belongs to**:

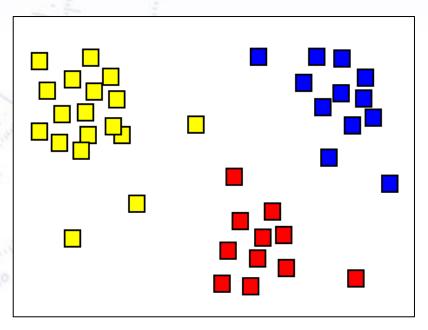
$$A = \sum_{c}^{clusters\ points} \sum_{p}^{clusters\ points} \operatorname{distance}(\overrightarrow{point}_{c,p} - \overrightarrow{cluster}_{c})$$

If A is small, this means that your points are well clustered.

To get an absolute scale, you can compare to B, calculated as the average distance to **all the other clusters**.

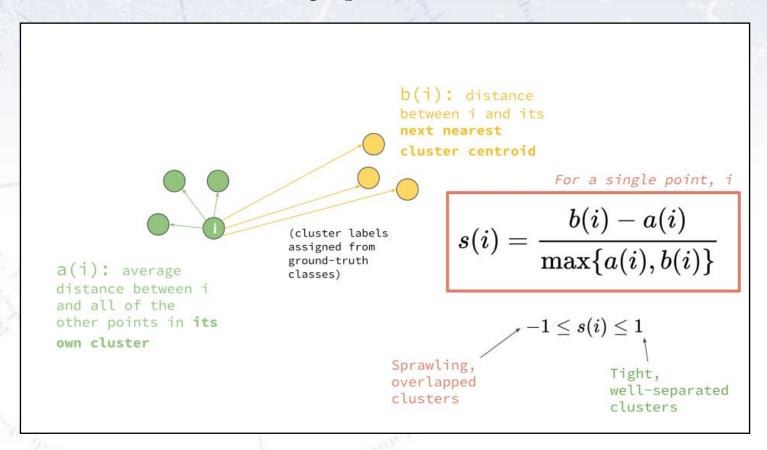
$$S = \frac{B - A}{max(A, B)}$$

This is called the Silhouette score.



Single point silhouette score

In addition to calculating a silhouette score for an overall algorithm result, it can also be calculated for a single point:



If you happen to have labels (perhaps for a subset), then you can calculate the performance using the <u>Adjusted Mutual Information Score</u> (link to SKLearn).

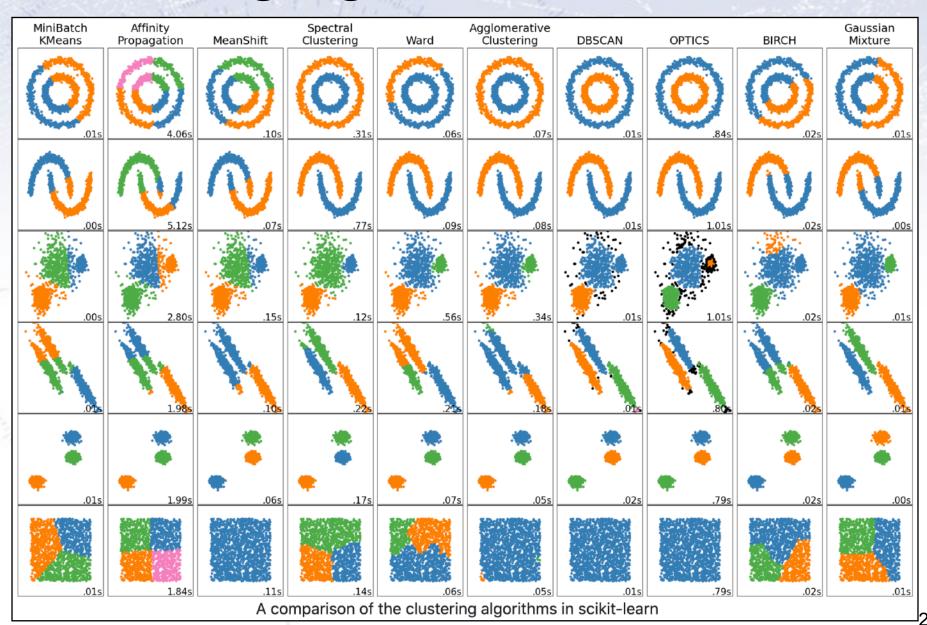
Clustering algorithms in scikit-learn

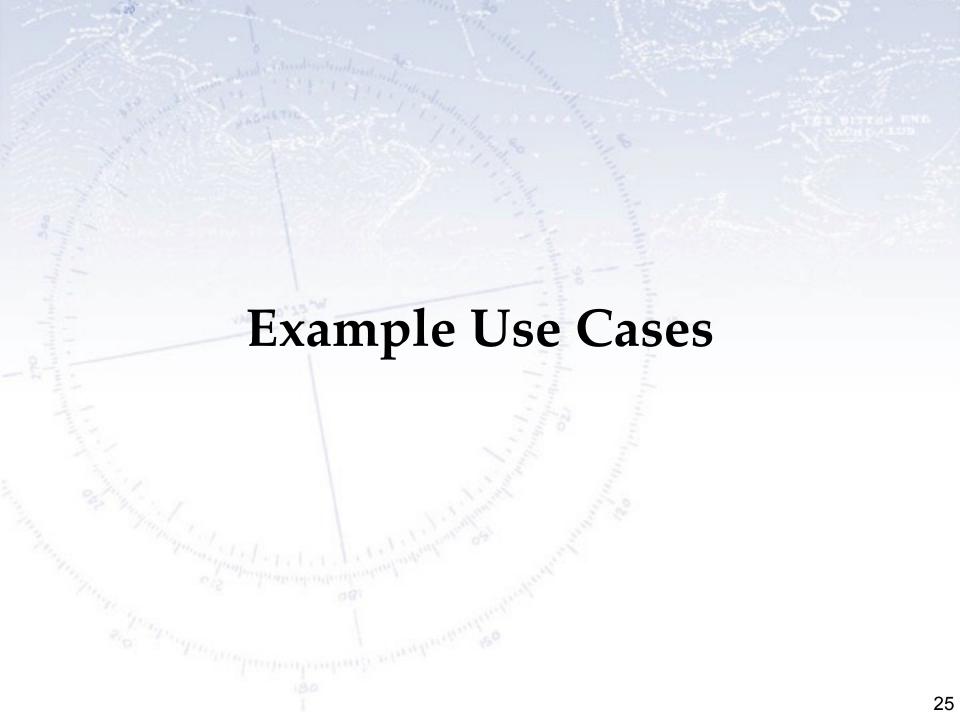
Scikit-Learn has a rather good selection of clustering algorithms:

Method name	Parameters	Scalability	Usecase	Geometry (metric used)
K-Means	number of clusters	Very large n_samples, medium n_clusters with MiniBatch code	General-purpose, even cluster size, flat geometry, not too many clusters, inductive	Distances between points
Affinity propagation	damping, sample preference	Not scalable with n_samples	Many clusters, uneven cluster size, non-flat geometry, inductive	Graph distance (e.g. near- est-neighbor graph)
Mean-shift	bandwidth	Not scalable with n_samples	Many clusters, uneven cluster size, non-flat geometry, inductive	Distances between points
Spectral clustering	number of clusters	Medium n_samples, small n_clusters	Few clusters, even cluster size, non-flat geometry, transductive	Graph distance (e.g. near- est-neighbor graph)
Ward hierarchical clustering	number of clusters or distance threshold	Large n_samples and n_clusters	Many clusters, possibly connectivity constraints, transductive	Distances between points
Agglomerative clustering	number of clusters or distance threshold, linkage type, distance	Large n_samples and n_clusters	Many clusters, possibly connectivity constraints, non Euclidean distances, transductive	Any pairwise distance
DBSCAN	neighborhood size	Very large n_samples, medium n_clusters	Non-flat geometry, uneven clus- ter sizes, outlier removal, transductive	Distances between near- est points
OPTICS	minimum cluster membership	Very large n_samples, large n_clusters	Non-flat geometry, uneven cluster sizes, variable cluster density, outlier removal, transductive	Distances between points
Gaussian mixtures	many	Not scalable	Flat geometry, good for density estimation, inductive	Mahalanobis distances to centers
BIRCH	branching factor, threshold, optional global clusterer.	Large n_clusters and n_samples	Large dataset, outlier removal, data reduction, inductive	Euclidean distance be- tween points

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Clustering algorithms in scikit-learn





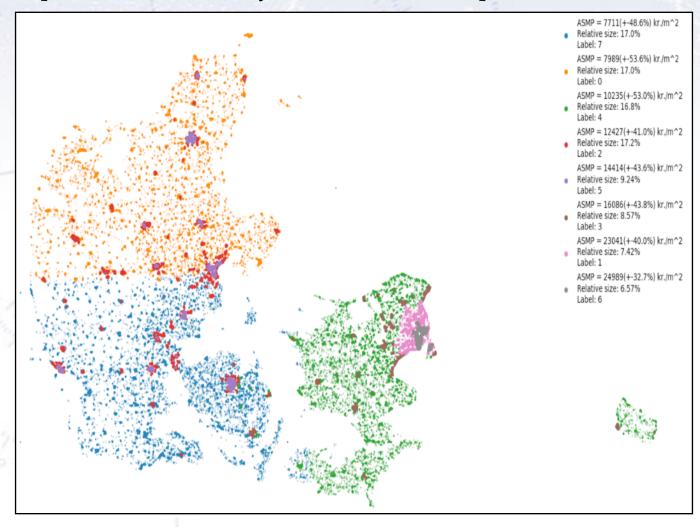
OK - what is it good for?

Clustering is used for several things:

- Market segmentation:
 Dividing costumers or products into similar classes is used in advertising.
- Production quality assurance:
 Clustering of images is used for detecting faulty productions automatically.
- DNA analysis: The ability to cluster very high dimensional data (DNA) to groups/families.
- Medical imaging:
 Classification of medical images without labels.
- Image segmentation:
 Dividing an image into its parts is used in e.g. self-driving and security.
- Anomaly detection: Quick detection of e.g. credit card fraud saves large amounts of money.

Clustering of Danish housing

Show is a simple clustering of the Danish housing market, based on position (x,y) and price/m2. In this way, one can see developments for each market.



"When I get new data, I always run a clustering and a dimension reduction algorithm on a random sample from it.

That only costs computing time, and might reveal things, that it would take me a long time to discover otherwise."

[Alexander, former student]

Conclusions

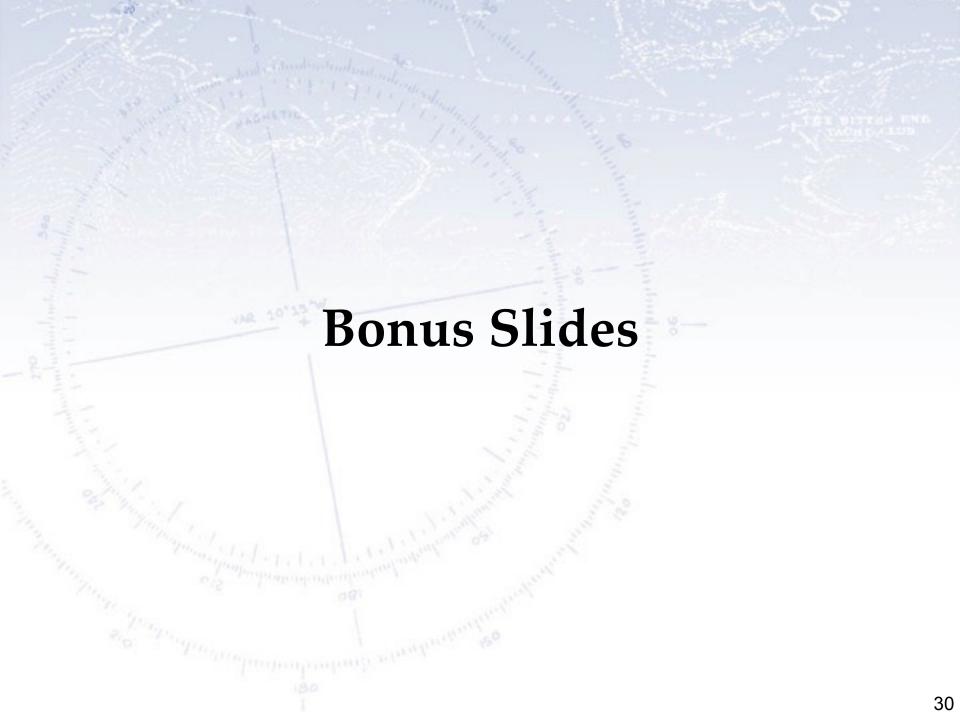
Clustering is an "old" art form, for which there is a vast ocean of methods.

K-means (and further developments) is the standard algorithm, if there is one such.

DBSCAN is also an old (and awarded!) classic. An updated version is called HDBSCAN.

Note that like in dimensionality reduction, it is important to transform the input variables first, so that mean and variances are of order zero and unity.

It is HARD to evaluate the performance, and visual inspection and testing on similar (typically simulated) cases are some of few methods.



k-Means clustering

