Applied Statistics Troels C. Petersen (NBI)

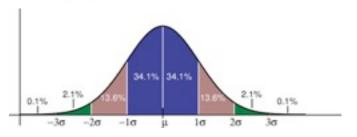






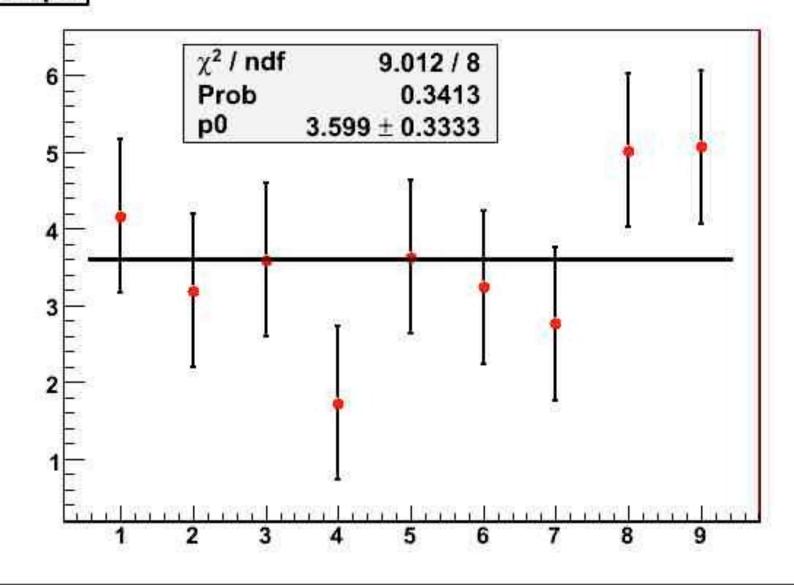






"Statistics is merely a quantization of common sense"

Graph ChiSquare method



Given data points (y_i as a function of x_i), how do you decide what fit/model best represents the data, and if this representation is good at all?

The answer: The ChiSquare...

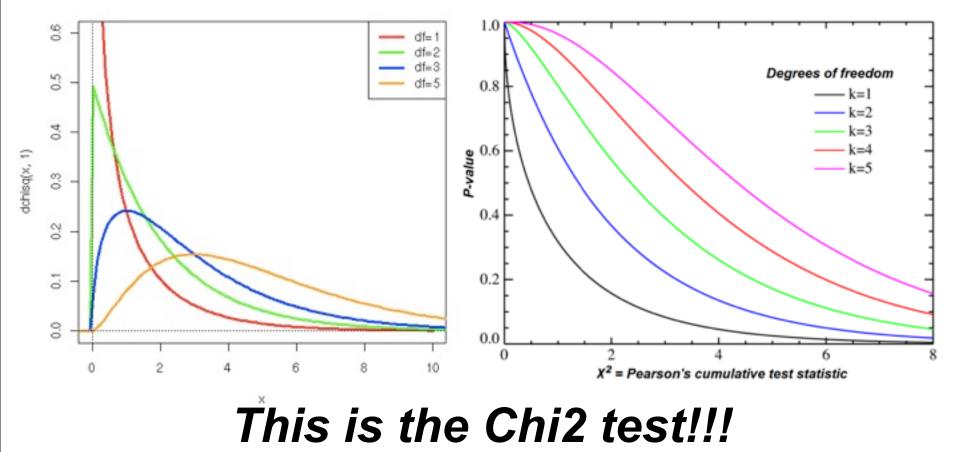
$$\chi^2(\bar{ heta}) = \sum_{i=1}^N \frac{(y_i - \lambda(x_i; \bar{ heta}))^2}{\sigma_i^2}$$

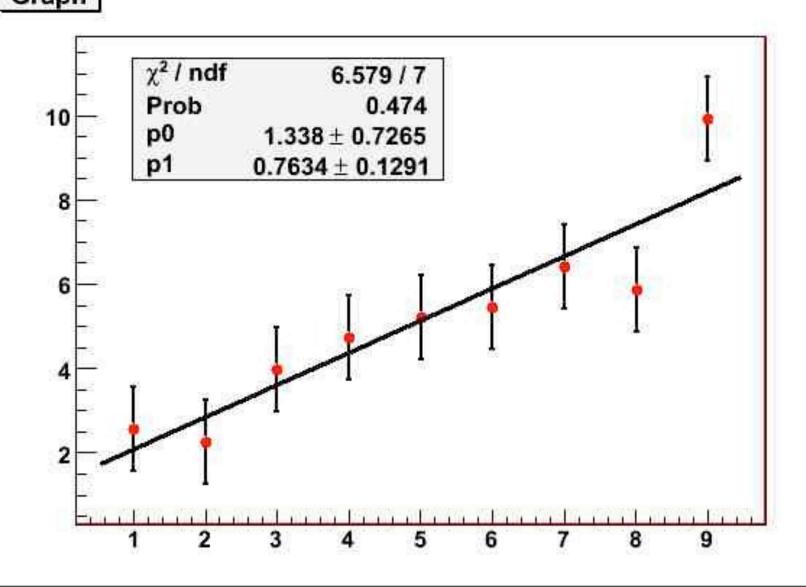
Take for every data point the difference between the value (y_i) and the fit (here λ) in terms of the uncertainty (σ_i) and square this. The goal is to *MINIMIZE* the sum of these terms!

From the value of the sum and the degrees of freedom, a fit quality can be calculated - *This is the Chi2 test!*

ChiSquare test

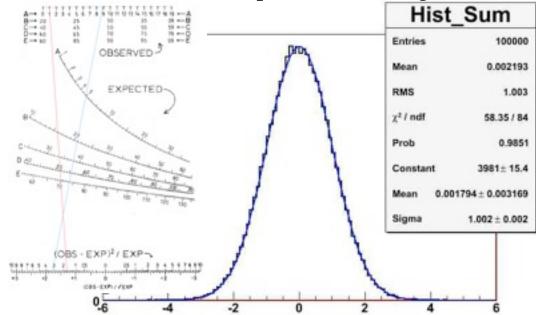
For a given number of degrees of freedom, the PDF for expected Chi2 values is known! Thus one can compare the obtained value to this, and calculate the probability of observing something with the same Chi2 value or higher...



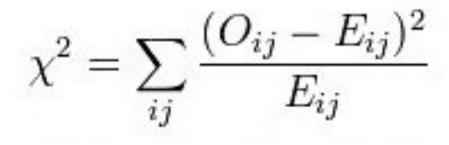


ChiSquare method for binned data

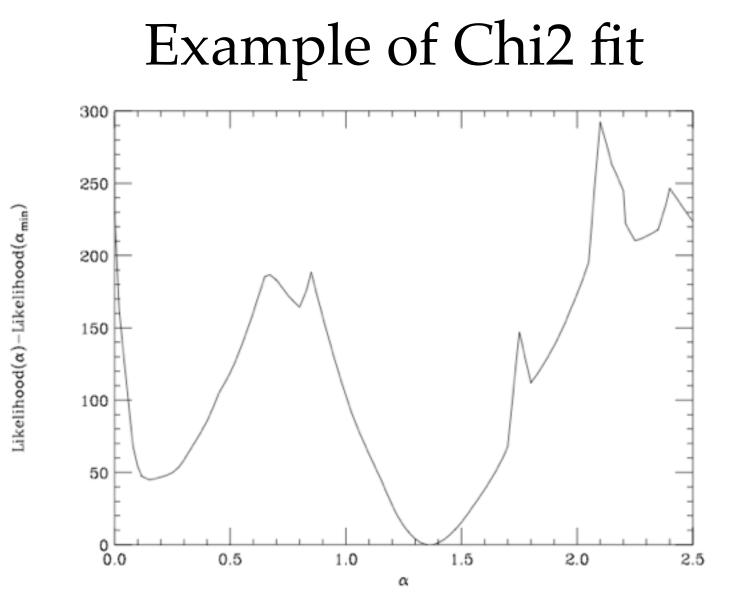
If the data is binned (i.e. put into a histogram), then Pearson's ChiSquare applies:



The formula (based on Poisson statistics) is:



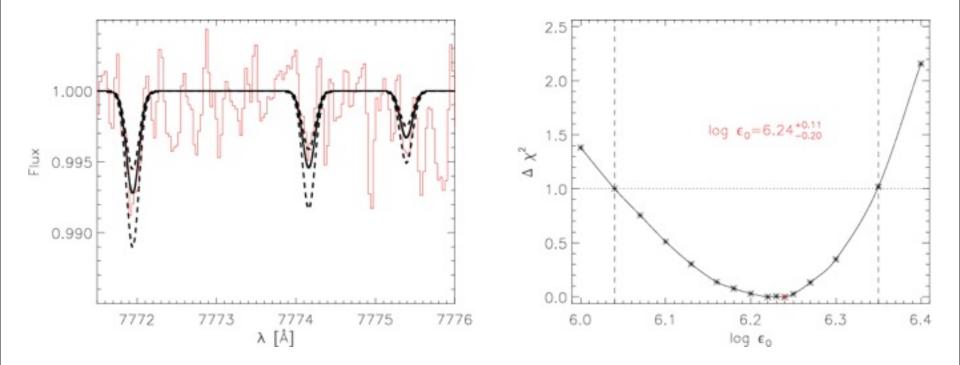




The fact that there are several minima makes fitting difficult/uncertain! *Always give good starting values!!!*

Example of Chi2 fit

Uncertainties need not always be symmetric (though that is usually better!)



The uncertainty on a parameter is found where the Chi2 has increased by 1 from the minimum.

Notes on the ChiSquare method

"It was formerly the custom, and is still so in works on the theory of observations, to derive the method of least squares from certain theoretical considerations, the assumed normality of the errors of the observations being one such. It is however, more than doubtful whether the conditions for the theoretical validity of the method are realized in statistical practice, and the student would do well to regard the method as recommended chiefly by its comparative simplicity and by the fact that it has **stood the test of experience**".

[G.U. Yule and M.G. Kendall 1958]

