Applied Statistics Troels C. Petersen (NBI)



Tuesday, September 6, 2011

Defining the mean

There are several ways of defining "a typical" value from a dataset:a) Arithmetic mean b) Mode (most probably) c) Median (half below, half above)d) Geometric mean e) Harmonic mean



Mean and width

It turns out, that the best estimator for the **mean** is (as you all know):

$$\hat{\mu} = \frac{1}{N} \sum x_i = \bar{x}$$

For the width of the distribution (a.k.a. standard deviation or RMS) it is:

$$\hat{\sigma} = \sqrt{\frac{1}{N} \sum (x_i - \mu)^2}$$

Note the "hat", which means "estimator". It is sometimes dropped...

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Relation between RMS and Gaussian width...

When a distribution is Gaussian, the RMS corresponds to the Gaussian width σ :



Mean and width

What is the **uncertainty on the mean?** And how quickly does it improve with more data?



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Weighted mean and width

What if we are given data, which has different uncertainties? How to average these, and what is the uncertainty on the average?

