Applied Statistics Why statistics?



Troels C. Petersen (NBI)



"Statistics is merely a quantization of common sense"

Why errors?!?

Errors/Uncertainties

In physics there are various elements of uncertainty:

- Theory is not deterministic Examples: Quantum effects & chaos
 Random measurement errors Fluctuations are present even without quantum effects!
- Things we could know in principle but don't... e.g. from limitations in cost, time, etc.

We can quantify the uncertainty using **PROBABILITY**

Armed with the realization of limitations, we can make better calculations/experiments and informed conclusions.

Example: Speed of Gravity

Imagine that you measured the speed of gravity, and got the following result:

$v_{\text{gravity}} = 2.89 \times 10^8 \text{ m/s}$

That would tell you...

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That would tell you...

Nothing!!!

Because you have no idea of the uncertainty.

Example: Speed of Gravity

Imagine that you measured the speed of gravity, and got the following result:

$$v_{\text{gravity}} = 2.89 \times 10^8 \text{ m/s}$$

Depending on the uncertainty, you might foresee three very different conclusions:

 $v_{\text{gravity}} = (2.89 \pm 9.21) \times 10^8 \text{ m/s}$ $v_{\text{gravity}} = (2.89 \pm 0.09) \times 10^8 \text{ m/s}$ $v_{\text{gravity}} = (2.89 \pm 0.01) \times 10^8 \text{ m/s}$

Could be anything, even negative!

Consistent with c, and not much else!

Inconsistent with c: New Discovery!!!

Numbers without stated uncertainties are meaningless!

Why precision?

Newton's Law of Gravity

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Valid for all masses? Force central? mMRange of validity? Square Law? No other dependencies?

Sunday, August 31, 14

Newton's Law of Gravity

How well do we know Newton's Law of Gravity? Well, reasonably well, but...

Valid for all masses? Force central? NO - not large ones! Seemingly... mMMaybe not short ranges Being tested Range of validity? Square Law? Yes, from generel relativity No other dependencies?

10

Sunday, August 31, 14



Why statistics?!?

Why statistics in physics?

Experimental measurements are only SAMPLES of the reality, they can never represent the entire set of possibilities, so → they are affected by uncertainties

 \rightarrow results can be expressed as probabilities

Theoretical calculations are mostly **APPROXIMATIONS** limited by finite resources to do the calculations or by imprecise input parameters, so

- \rightarrow they are also affected by uncertainties
- → predictions can also be expressed in terms of probability

Statistics gives the understanding of **uncertainty** and **probability** in relating data and theory!!!

Why statistics in physics?

Statistics is about hypothesis testing, quantifying the answer to the question "which theory matches the data best?"

Statistics is about fitting trends in data, allowing for projections and predictions.

Statistics is about collecting data and logically analyzing it, not being fooled by coincidences and chance observations.

Statistics is about understanding data, and extracting the essential information from it in the most powerful way.



Biases in statistics...

When ASKING people, one may introduce (deliberate?) biases:

- *Wording* 1: Pick a color: red or blue?
- *Wording* **2**: Pick a color: blue or red?

Color Choice	Red	Blue
Wording 1	59%	45%
Wording 2	41%	55%

One may also bias answers by giving (ir-)relevant information:

- *Wording* 1: Knowing that the population of the U.S. is 270 million, what is the population of Canada?
- *Wording* **2:** Knowing that the population of Australia is 15 million, what is the population of Canada?



Sunday, August 31, 14

Mark Twain: "There are three kinds of lies: lies, damned lies, and statistics."

My opinion: *"The only way to convey accurate information is by statistics."*





Big Data's High-Priests of Algorithms

'Data Scientists' Meld Statistics and Software for Find Lucrative High-Tech Jobs 8th of August 2014

While a six-figure starting salary might be common for someone coming straight out of a doctoral program, data scientists with just two years' experience can earn between \$200,000 and \$300,000 a year, according to recruiters.

"I keep saying the sexy job in the next ten years will be statisticians."

[Hal Varian in 2009, Chief economist of Google, Berkeley professor]

